Math 95, (Instructor: Mr. Diss) Final Test: Do all steps on separate paper. Please do not write on this sheet. Please work in a vertical format and skip lines between problems.

1. Given the function, $f(x)=x^{2}+x+4$, complete the following:
a. Solve $f(x)=16$
b. Evaluate $f(-3)$.
c. Simplify $3 f(x)$
2. Factor completely.
a. $\quad 6 x^{2}-13 x-8$
b. $3 x^{3}-36 x^{2}+33 x$
c. $x^{2}+x-24$
3. Solve the following and include steps for finding the LCD and include steps for the restrictions.
$\frac{1}{x^{2}-16}+\frac{4}{x+4}=\frac{5}{x-4}$
4. Simplify the following. Make sure you include hidden restrictions.

$$
\frac{x+5}{x^{3}-x} \div \frac{x^{2}-25}{x^{3}}
$$

5. Simplify the following. Make sure you include hidden restrictions.

$$
\frac{2}{x^{2}-1}-\frac{2}{x-1}
$$

6. Solve the following worded problems:
a. Use the formula $d \approx 1.22 \sqrt{h}$, where $d$ is distance in miles a person can see out to the horizon at a height, $h$, where $h$ is in feet. Solve the equation for $h$ [Hint: Square both sides of the equation]. Determine the height of the viewer if they want to see out to a distance of 10 miles.
b. One machine cuts the metal in 12 minutes and the second machine can cut the metal in 6 minutes. How long would it take to cut the metal if both machines work together?
7. Solve and check.
$\sqrt{5 x-1}=\sqrt{x+1}$
8. Answer the following on functions. [Note: Approximate values may be used.]

a. Find $g(-12)$.
b. Find $g(4)$.
c. Solve $g(x)=5$.
d. Solve $g(x)=-3$.
e. State the domain and range of $g(x)$ in interval notation.
9. Solve by completing the square and by using the quadratic formula and answers from both methods should be the same.

$$
3 x^{2}-2 x=2
$$

10. Put the following function, $f(x)=-x^{2}-2 x+8$ in vertex form by competing the square, and then do the following:

- Write down the open direction
- Write the Vertex
- Axis of symmetry
- Find the y intercept
- Find the x intercepts
- Graph and show the axis of symmetry in a dashed line.

